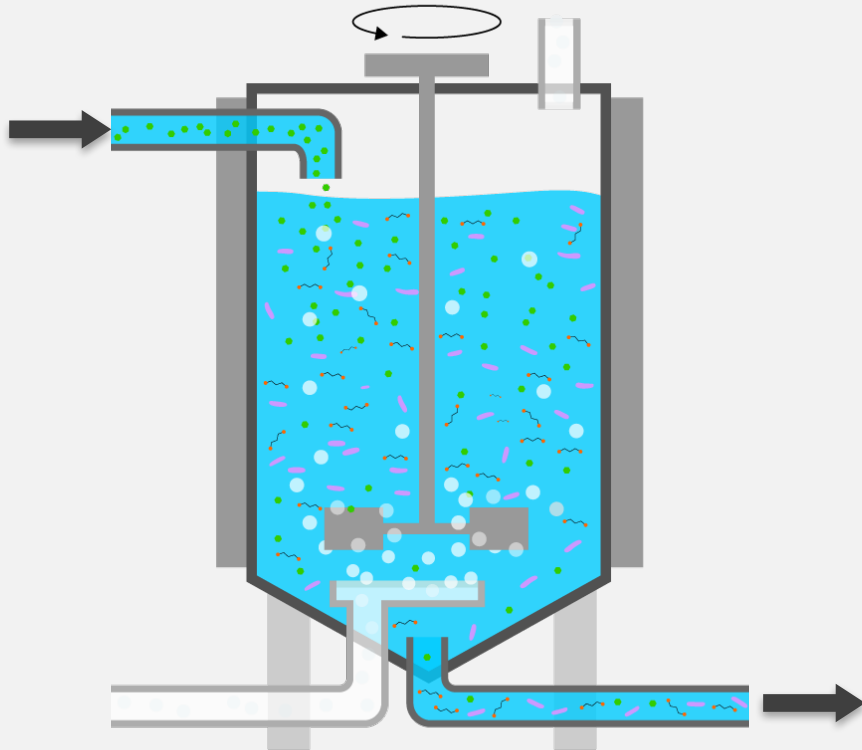


# Learning about the process and organism: Batch

Sef Heijnen, Department of Biotechnology, Faculty of Applied Sciences

## Chemostat

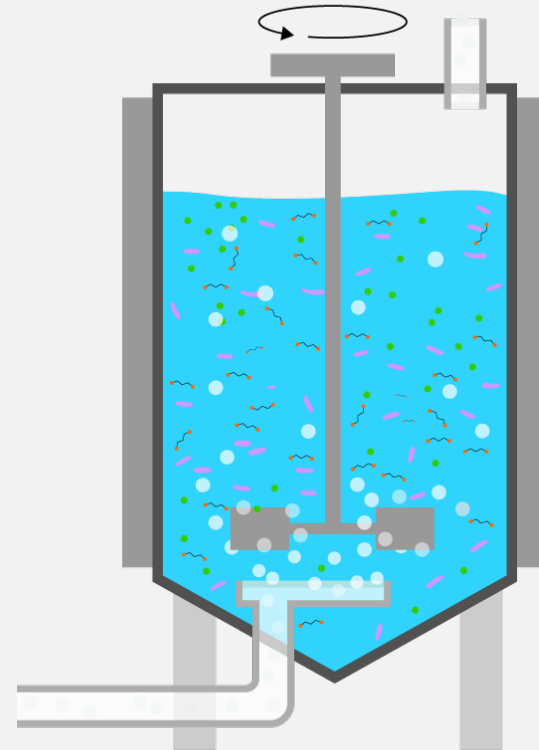
Control over  $\mu$ ,  $q_s$  and  $q_p$



Volume: constant

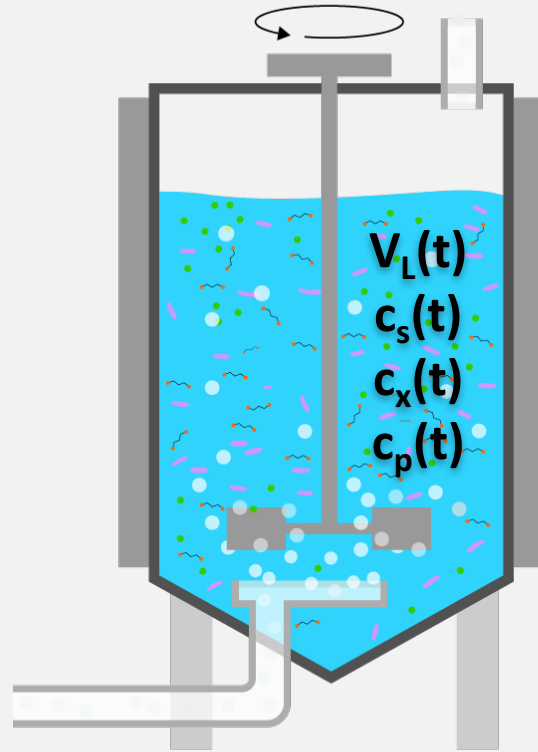
## Batch

$\mu$ ,  $q_s$  and  $q_p$ ?



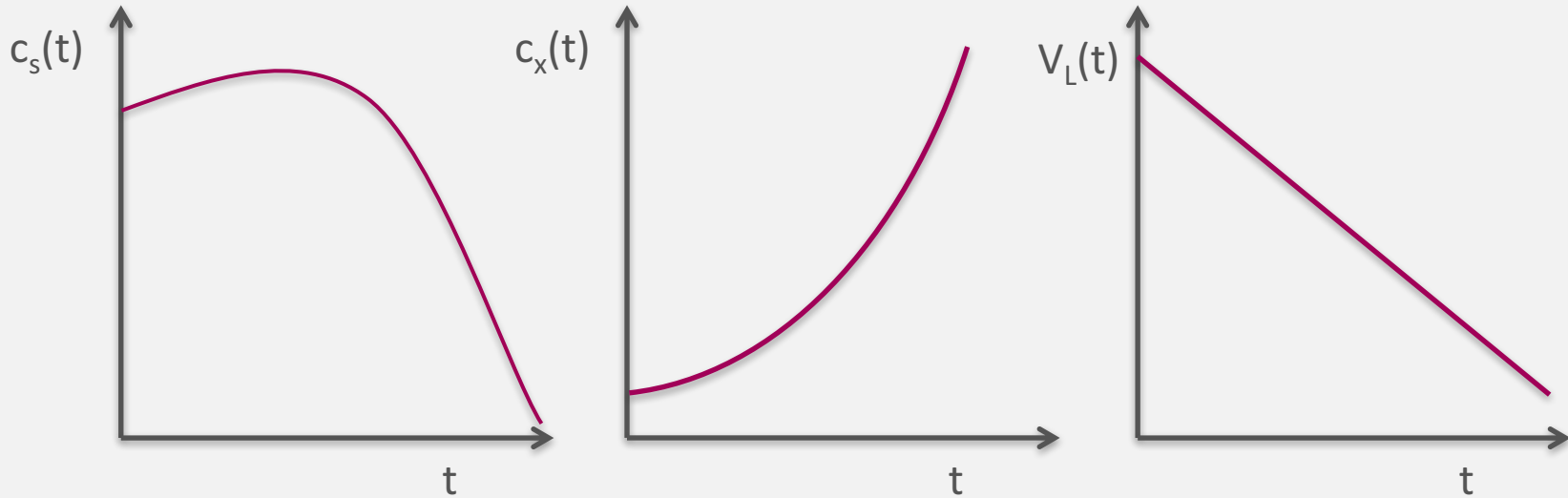
Volume: not constant

# Broth balances in batch



All time dependent

# Batch volume changes in time



Volume change: water evaporation, pH-titrant addition

# Broth balances in batch

**Biomass:**

$$\frac{d(V_L(t)c_x(t))}{dt} = \mu(t)V_L(t)c_x(t)$$

Accumulation

Conversion

**Substrate:**

$$\frac{d(V_L(t)c_s(t))}{dt} = q_s(t)V_L(t)c_x(t)$$

Accumulation

Conversion

NO STEADY STATE

TIME DEPENDENT CONCENTRATIONS

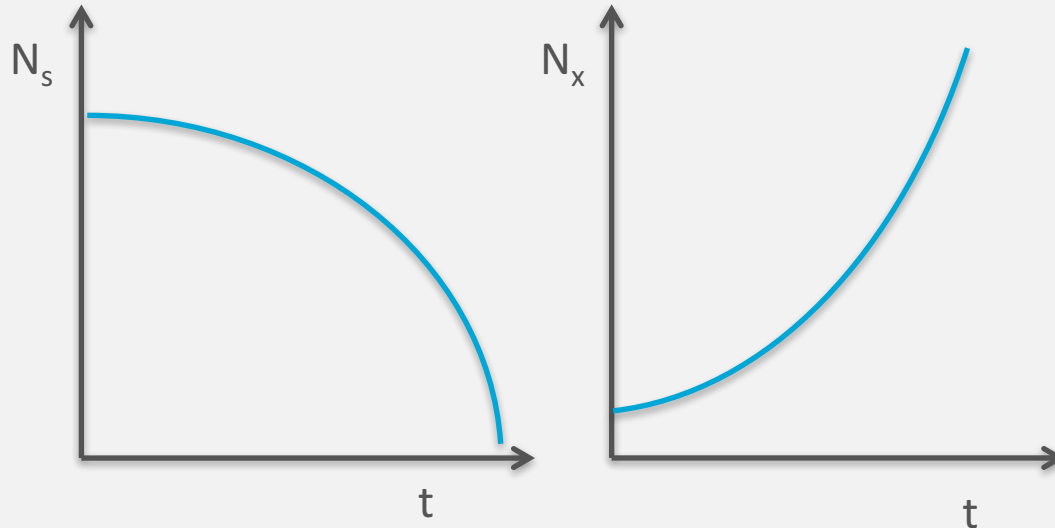
$$N_x(t) = V_L(t)c_x(t)$$

$$\frac{dN_x(t)}{dt} = \mu(t)N_x(t)$$

$$N_s(t) = V_L(t)c_s(t)$$

$$\frac{dN_s(t)}{dt} = q_s(t)N(t)$$

In batch we look at amounts  $N_i$



# Obtaining $\mu$ from a batch experiment: Set up the biomass balance

**Biomass balance:**

$$\frac{dN_x(t)}{dt} = \mu(t)N_x(t)$$

3 variables

$(N_x(t), t, \mu(t))$

**UNSOLVABLE**

$$\mu(t) = \mu_{max}$$

$$\frac{dN_x(t)}{dt} = \mu_{max}N_x(t)$$

2 variables  $(N_x(t), t)$

1 parameter  $(\mu_{max})$

**SOLVABLE**

# Obtaining $\mu$ from a batch experiment: Solve the biomass balance

$$\frac{dN_x(t)}{dt} = \mu_{max} N_x(t)$$

$$\frac{1}{N_x(t)} dN_x(t) = \mu_{max} dt$$

$$\int_{N_x(0)}^{N_x(t)} \frac{1}{N_x(t)} dN_x(t) = \mu_{max} \int_{t_0}^t dt$$

Separating variables

Setting integral and initial values

INTEGRATION

$$\ln \frac{N_x(t)}{N_x(0)} = \mu_{max} t$$

Log-linear

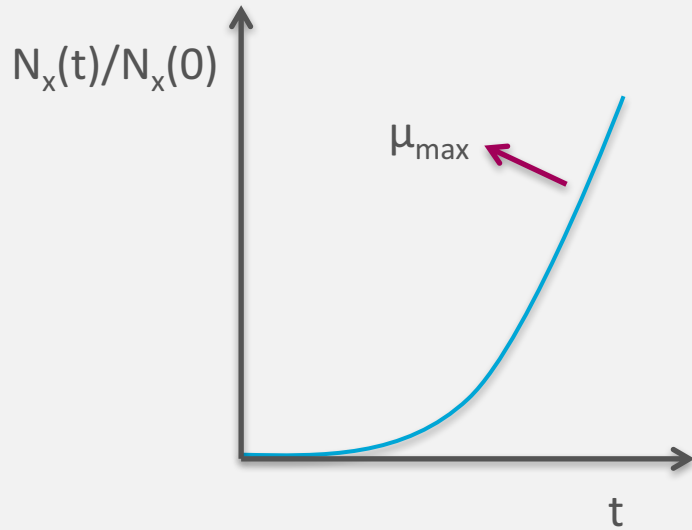
or:

$$N_x(t) = N_x(0) e^{\mu_{max} t}$$

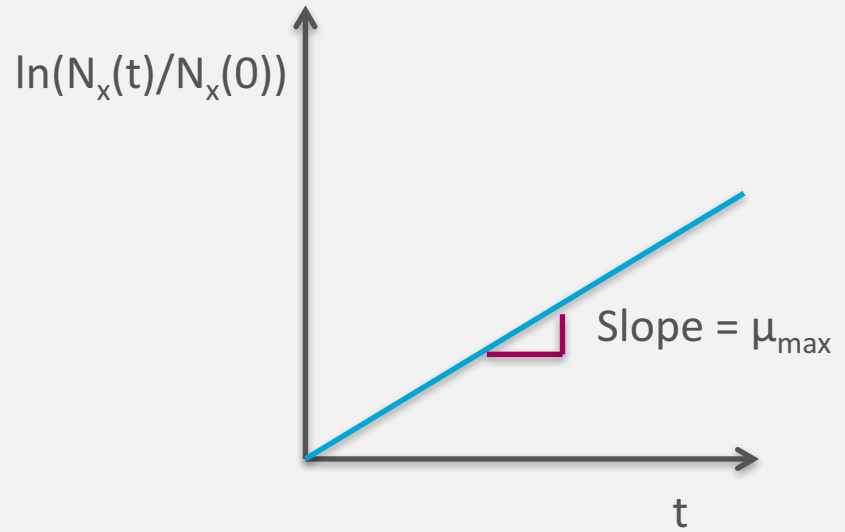
Exponential



# Obtaining $\mu_{\max}$ : Non-linear data fitting to $N_x(t)$



Exponential relation



Log-linear growth relation

# Obtaining $q_{s,max}$ : solving the substrate balance

Substrate balance:

$$\frac{dN_s(t)}{dt} = q_{s,max} N_x(t)$$

Biomass balance:

$$\frac{dN_x(t)}{dt} = \mu_{max} N_x(t)$$

COMBINE

$$\frac{dN_s(t)}{dt} = \frac{q_{s,max}}{\mu_{max}} \frac{dN_x(t)}{dt}$$

$$\int_{N_s(0)}^{N_s(t)} dN_s(t) = \frac{q_{s,max}}{\mu_{max}} \int_{N_x(0)}^{N_x(t)} dN_x(t)$$

Setting integral and initial values

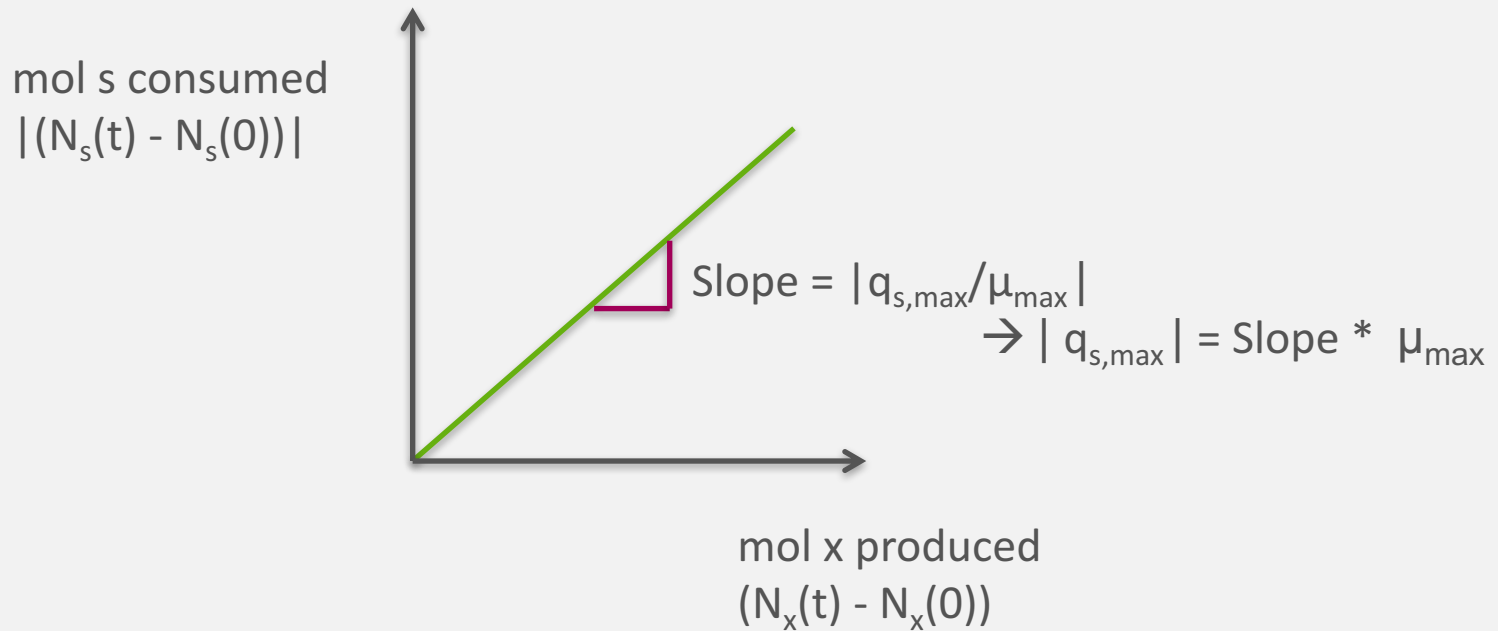
INTEGRATION

$$(N_s(t) - N_s(0)) = \frac{q_{s,max}}{\mu_{max}} (N_x(t) - N_x(0))$$

Consumed substrate

Produced biomass

# Obtaining $q_{s,max}/\mu_{max}$ : linear data fitting



## Wrap up:

# Learning about the process and organism: Batch

### We have learned about the batch that:

- Batch broth volume seldom constant in time
- Balances show: use amounts, not concentrations
- Biomass balance
  - Biomass growth is exponential in time
  - Allows to calculate  $\mu_{\max}$
- $q_{s,\max}$  and  $q_{p,\text{batch}}$  found through combi-balances
- Combi-balances show that linear plots of consumed  $s$  or produced  $p$  against produced  $x$  should be made

See you in the next unit!